

Main Talks IV Seminar on Categories and Applications Bellaterra, 6 to 9 of June of 2007

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Functor category associated to quadratic spaces over \mathbb{F}_2

The category F(p) of functors from the category Ef of finite Fp-vector spaces to the category E of all \mathbb{F}_p -vector spaces is connected to several areas of mathematics. An important algebraic motivation for the particular interest in the category F(p) follows from the link with the modular representation theory and the cohomology of finite general linear groups. A fundamental result obtained by Betley-Suslin relates the calculation of extension groups in the category $\mathcal{F}(p)$ with certain stable cohomology groups of general linear groups. It is natural to seek to construct other categories of functors that play a similar role for other families of algebraic groups and, in particular, for the orthogonal groups.

In this talk I will explain the construction of the functor category \mathcal{F}_{quad} , which has some good properties as a candidate for the orthogonal group over the field with two elements and I will give several results about the structure of this category.

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