

Short Communications IV Seminar on Categories and Applications Bellaterra, 6 to 9 of June of 2007

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Completeness of cocompletions in enriched category theory

(Joint work with J. Velebil.) We study the existence of limits of a certain class L inside the cocompletion C(A) of a V-category A under a class of colimits C, where V is a symmetric monoidal closed category that is locally finitely presentable as such. We investigate conditions that are equivalent to the existence of L-limits of representables inside the C-cocompletion of a category and we exploit them in order to characterize the L-completeness of C(A) for particular classes C and L. Some well-known conditions for additive categories and posets arise from our analysis, while we obtain a (seemingly new) characterization of the small completeness of the inductive completion of both an ordinary category as well as of a category enriched in simplicial sets.

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