

Strange chaotic triangular maps

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- $(X, \rho) \dots$ compact metric space
- $f \in C(X) \dots$ continuous map $f : X \rightarrow X$
- $I = [0, 1]$
- triangular map \dots a continuous map $F : I^2 \rightarrow I^2$ of the form $F(x, y) = (f(x), g_x(y))$
- $\mathcal{T} \dots$ the class of triangular maps

- A map $f \in C(X)$ is of type 2^∞ if it has a periodic orbit of period 2^n for every $n \in \mathbb{N}$, and has no other periodic orbits.

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For $f \in C(I)$:

$$h(f) = 0 \Leftrightarrow f \text{ is of type } \leq 2^\infty$$

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